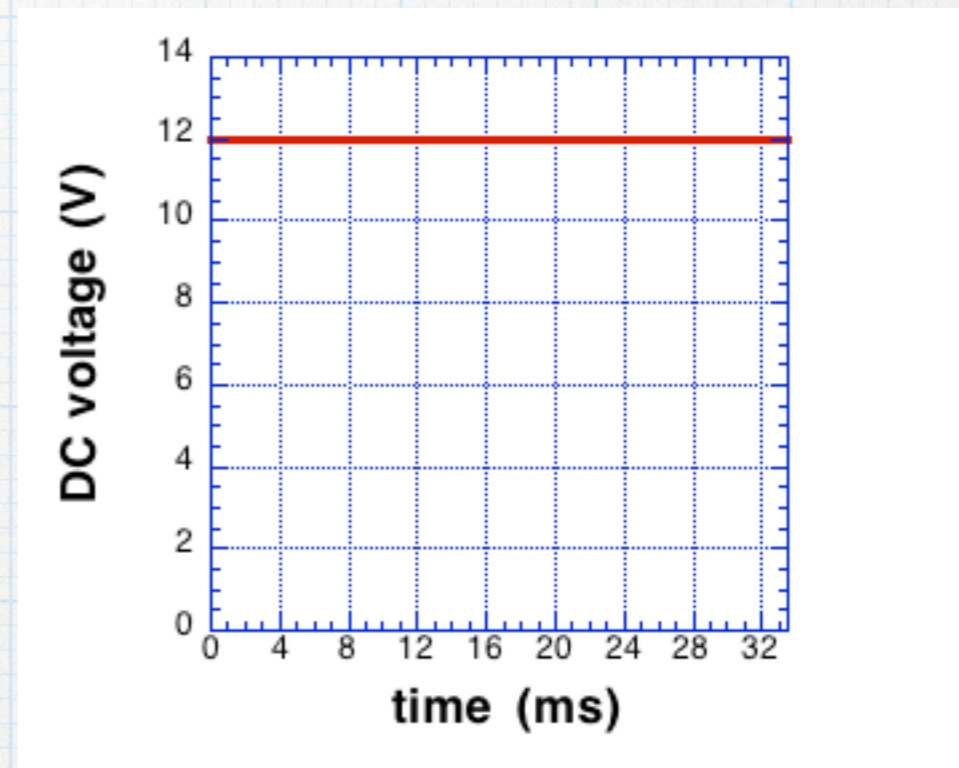
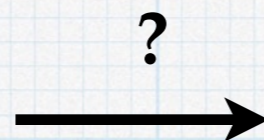
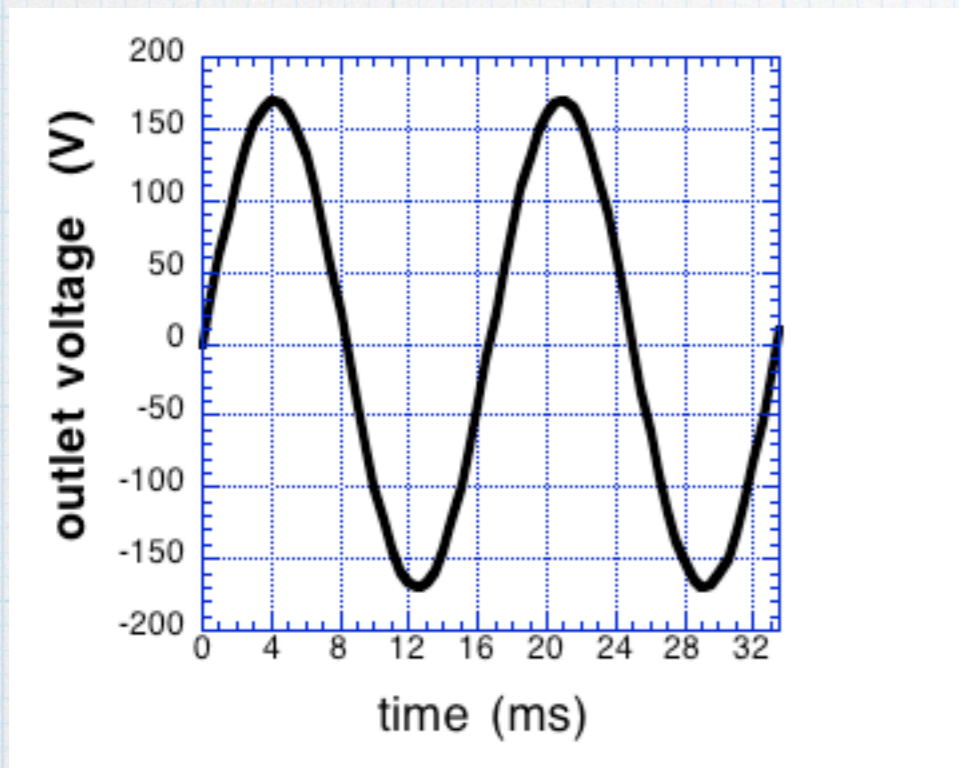


Rectifier circuits & DC power supplies

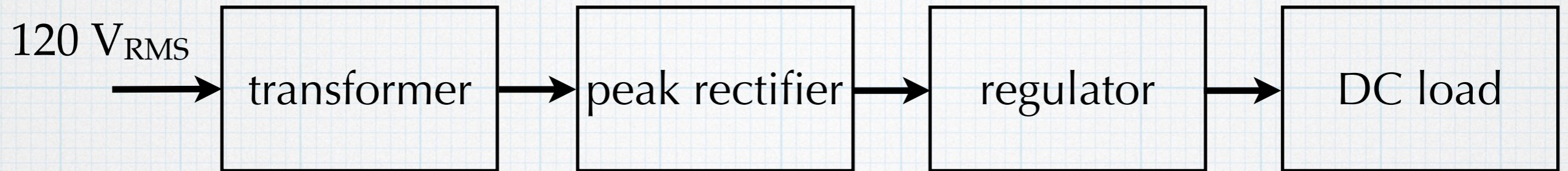
Goal: Generate the DC voltages – needed for most electronics – starting with the AC power that comes through the power line.



$$120 V_{\text{RMS}} \quad f = 60 \text{ Hz} \quad (T = 16.67 \text{ ms})$$

$$V_{ac} = (170\text{V}) \sin\left(\frac{2\pi}{T}t\right)$$

How to take time-varying voltage with an average value of 0 and turn it into a DC voltage?



transformer : reduces AC amplitude to something safe and manageable.
 V_{peak} from the transformer will be a few volts bigger than the desired DC voltage.

peak rectifier : breaks up the AC waveform and produces a $V_{DC} \approx V_{peak}$.

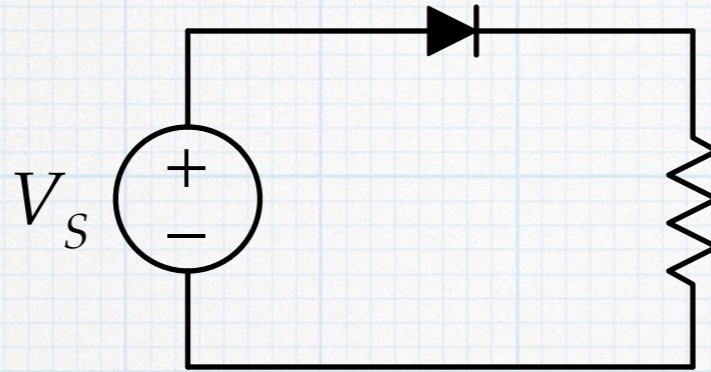
regulator : Refines the output of the rectifier. (optional)

Issues:

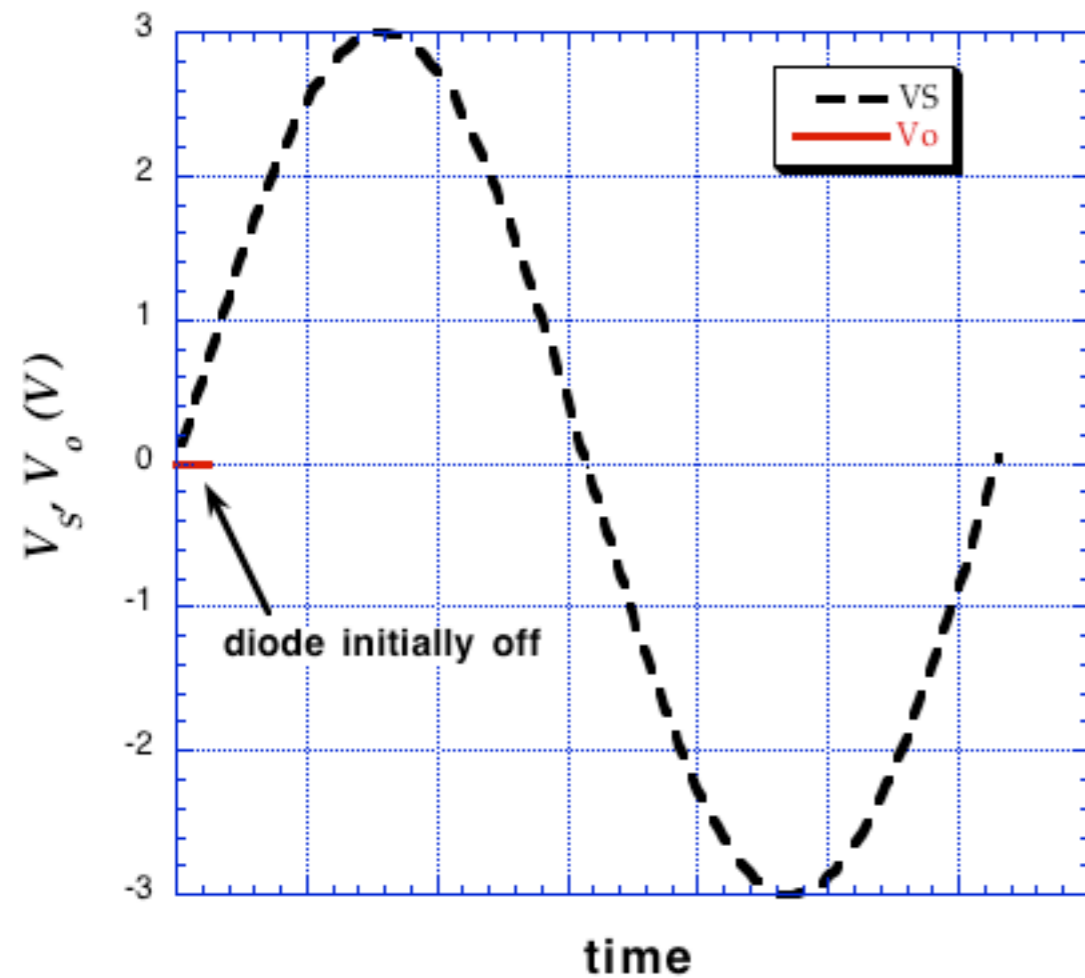
- Total power
- Efficiency
- Cost
- Load regulation (Does V_{DC} change as the load draws different amounts of current?)
- Line regulation (Does V_{DC} change if the input AC amplitude changes?)

Half-wave rectifier

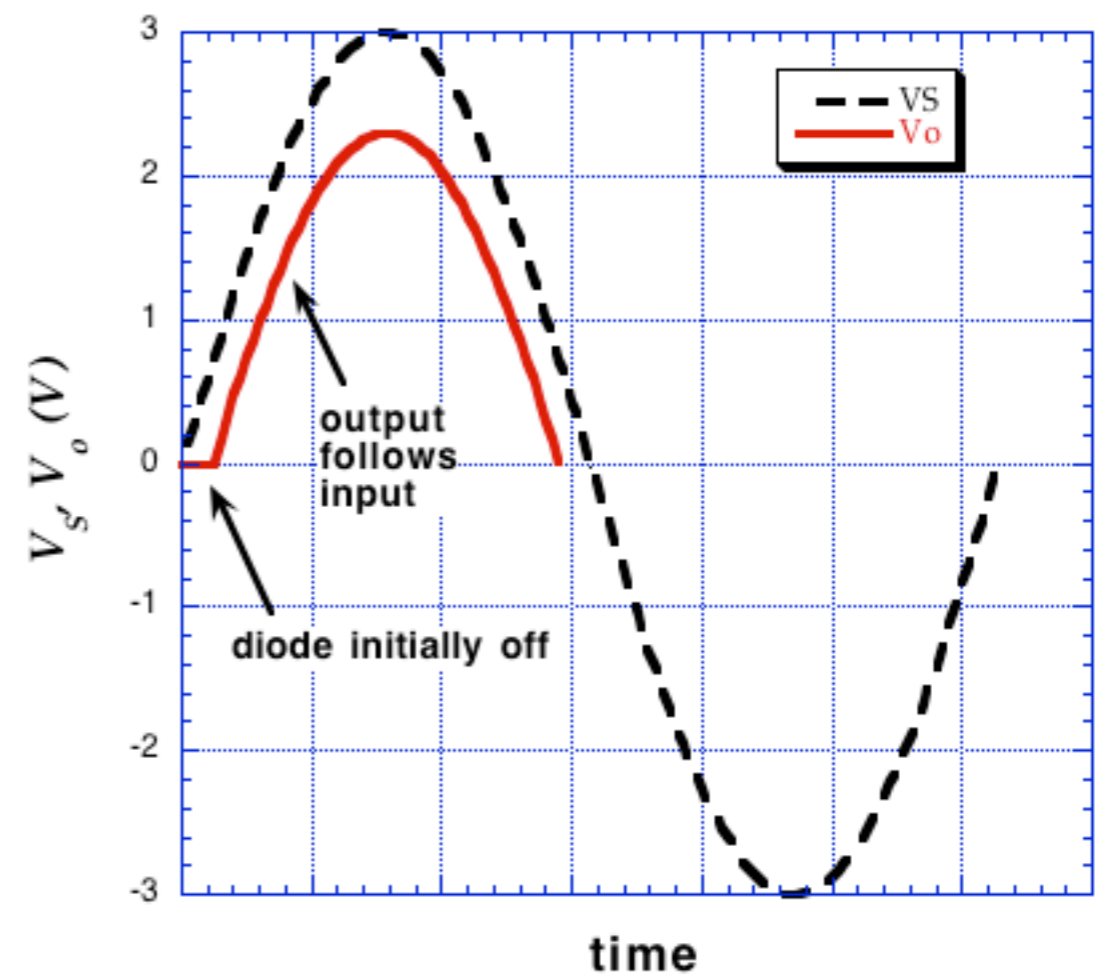
$$V_S(t) = V_p \sin\left(\frac{2\pi}{T}t\right)$$
$$V_p = 3 \text{ V.}$$



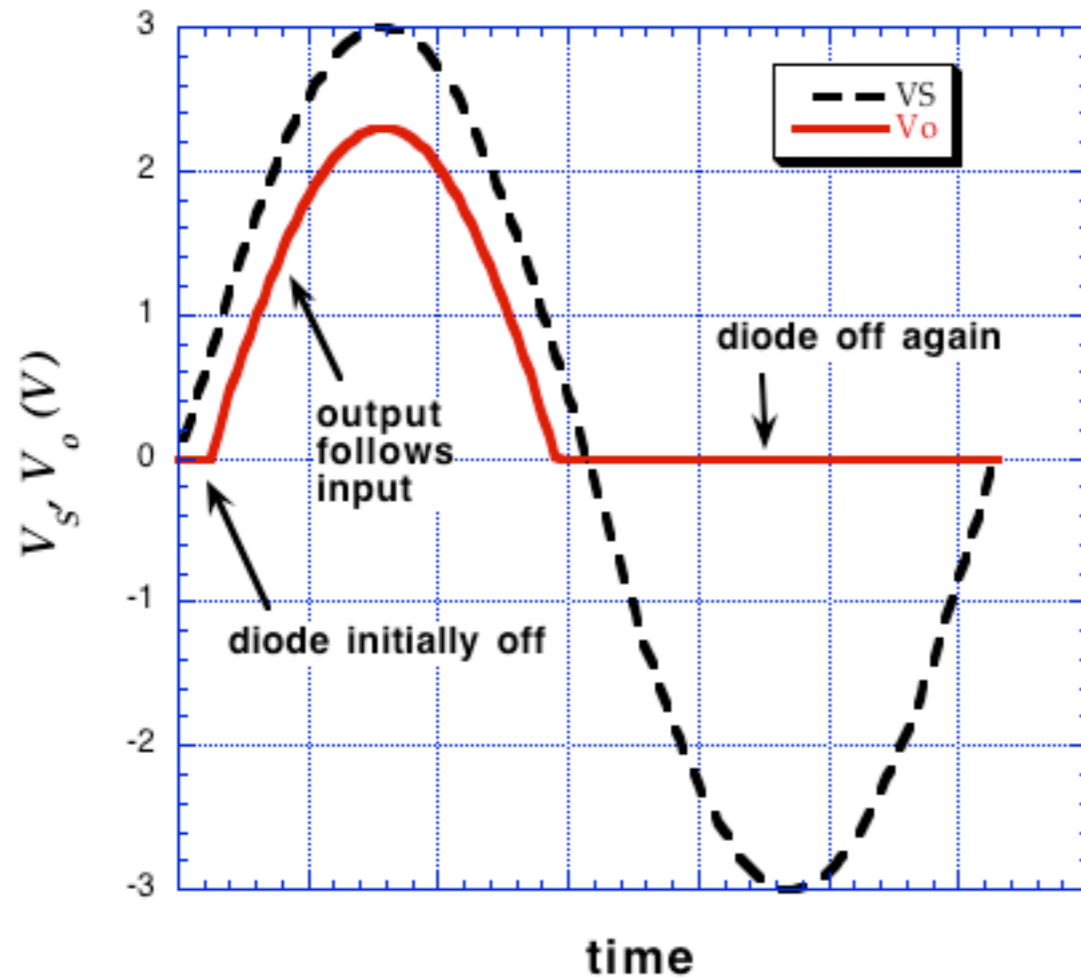
+ Resistor represent a load.
 v_R We are trying to deliver
- DC power to the load.



Diode is off until $V_S > 0.7 \text{ V}$.



Current flows when diode is in forward conduction. The output tracks the input during positive half cycle.



The diode turns off when $V_S < 0.7 \text{ V}$. It stays off during the negative half cycle of the sinusoid.

$$\begin{aligned}
 V_S > 0: \quad v_R(t) &\approx V_p \sin\left(\frac{2\pi}{T}t\right) - 0.7\text{V} & V_o(\text{avg}) &\approx \frac{V_P}{\pi} - \frac{0.7\text{V}}{2} \\
 V_S < 0: \quad v_R(t) &= 0: & & \neq 0!
 \end{aligned}$$

To get the negative half of the cycle, turn the diode around.

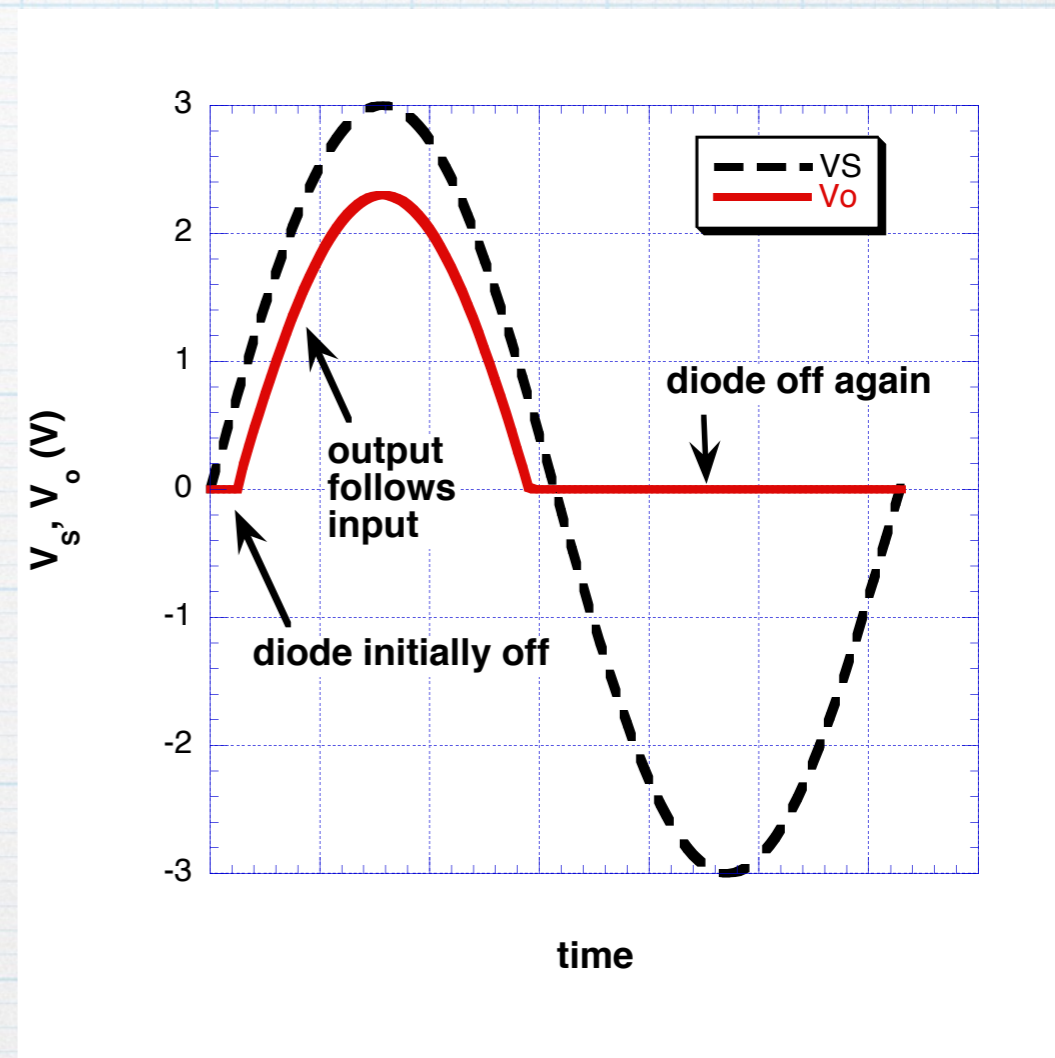
Time delay

Note that since the diode will not turn on until the sinusoid goes above $\approx 0.7\text{ V}$, there is time delay before the rectifier “turns on”. It is a simple matter to determine the delay time, using the “on-off” diode model:

$$0.7\text{V} = V_p \sin\left(\frac{2\pi}{T}t'\right)$$

$$t' = \frac{T}{2\pi} \arcsin\left(\frac{0.7\text{V}}{V_p}\right)$$

If $f = 60\text{ Hz}$ ($T = 16.67\text{ ms}$)
and $V_p = 3\text{ V}$, $t' = 0.62\text{ ms}$.

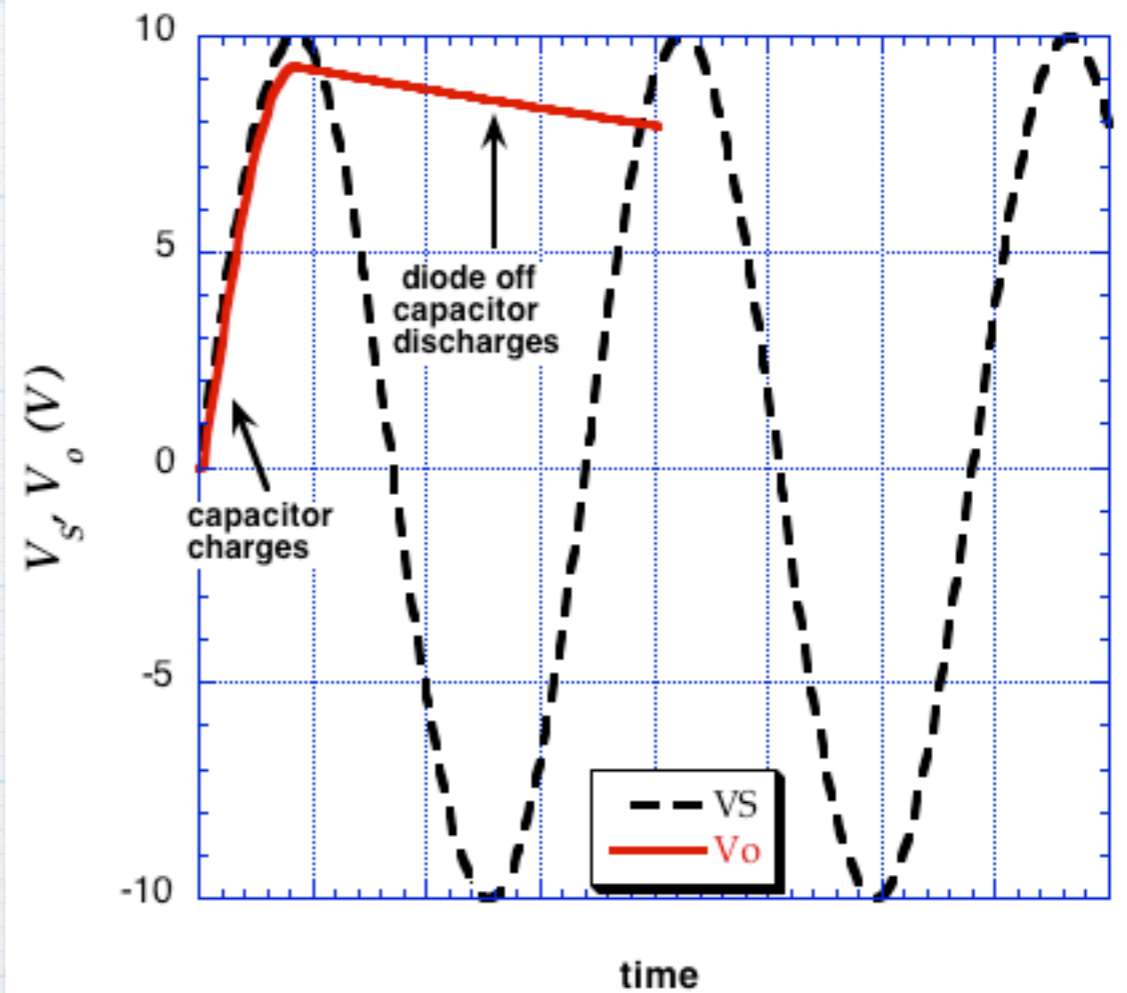
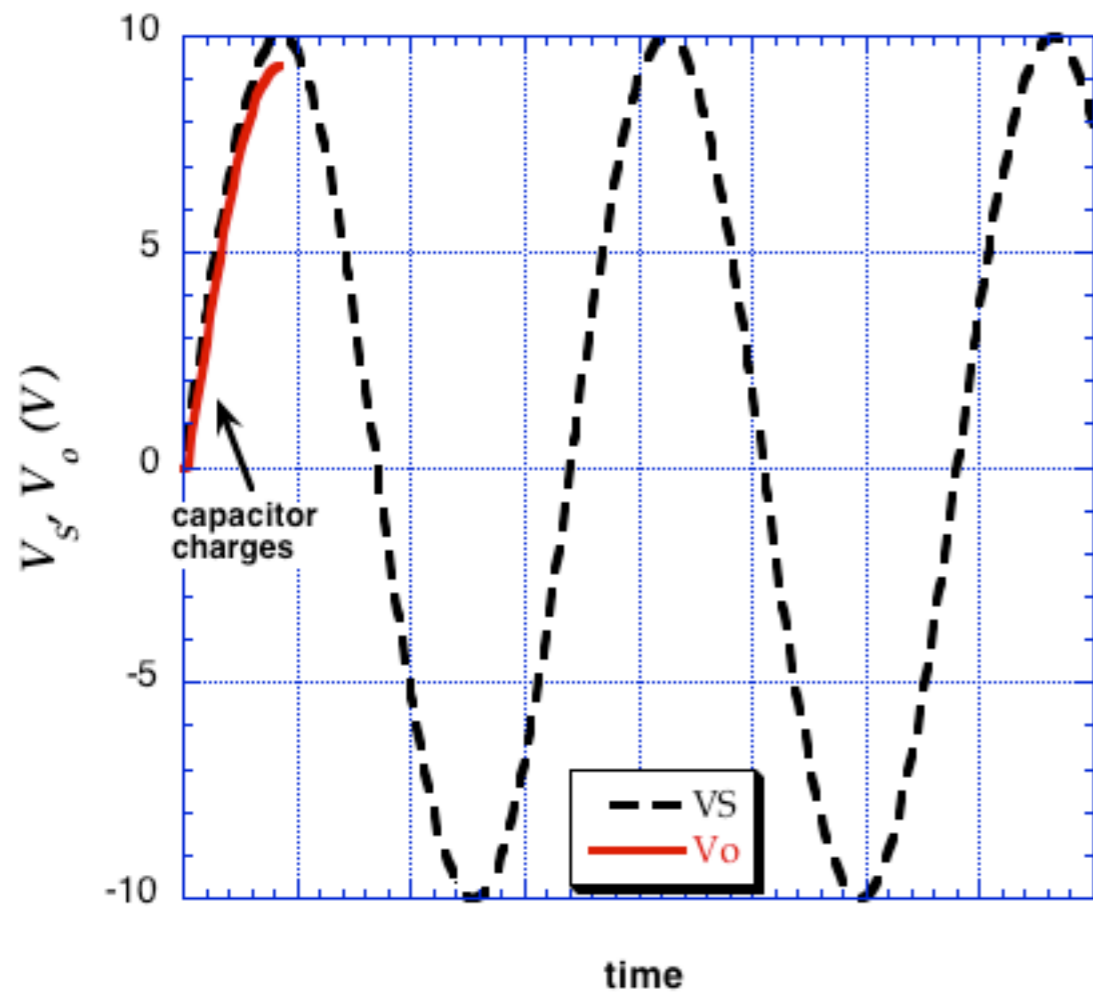
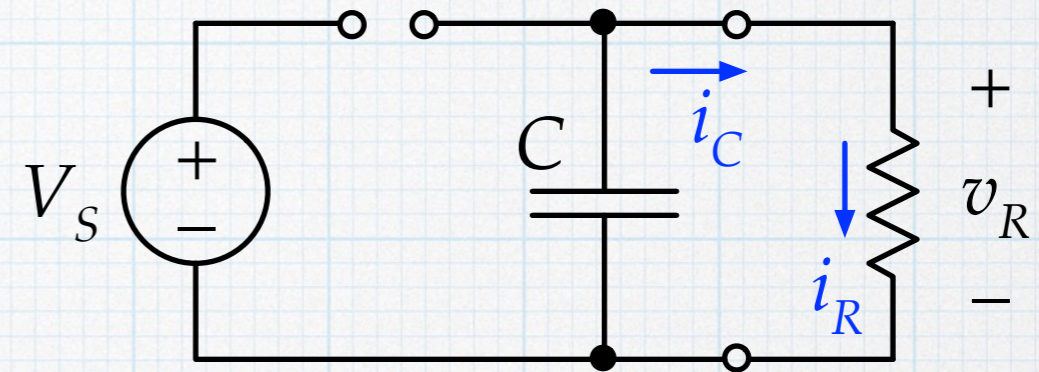
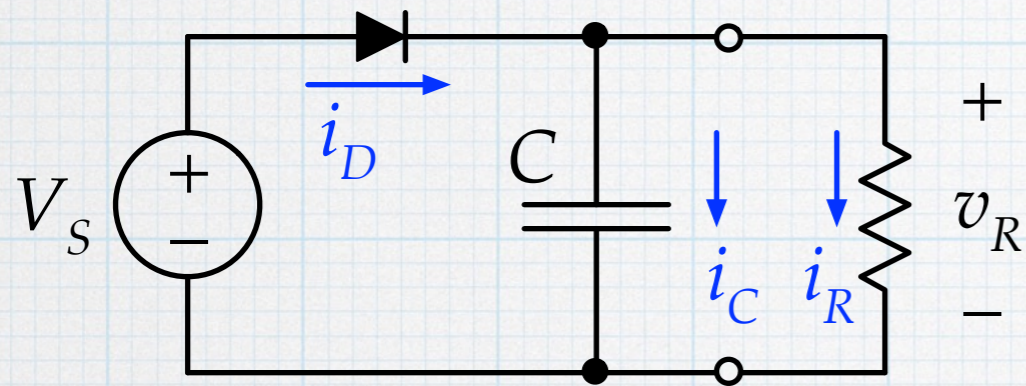


There is a similar time offset at the other end of the positive half cycle.

The effect of the time offset become negligible if $V_p \gg 0.7\text{ V}$.

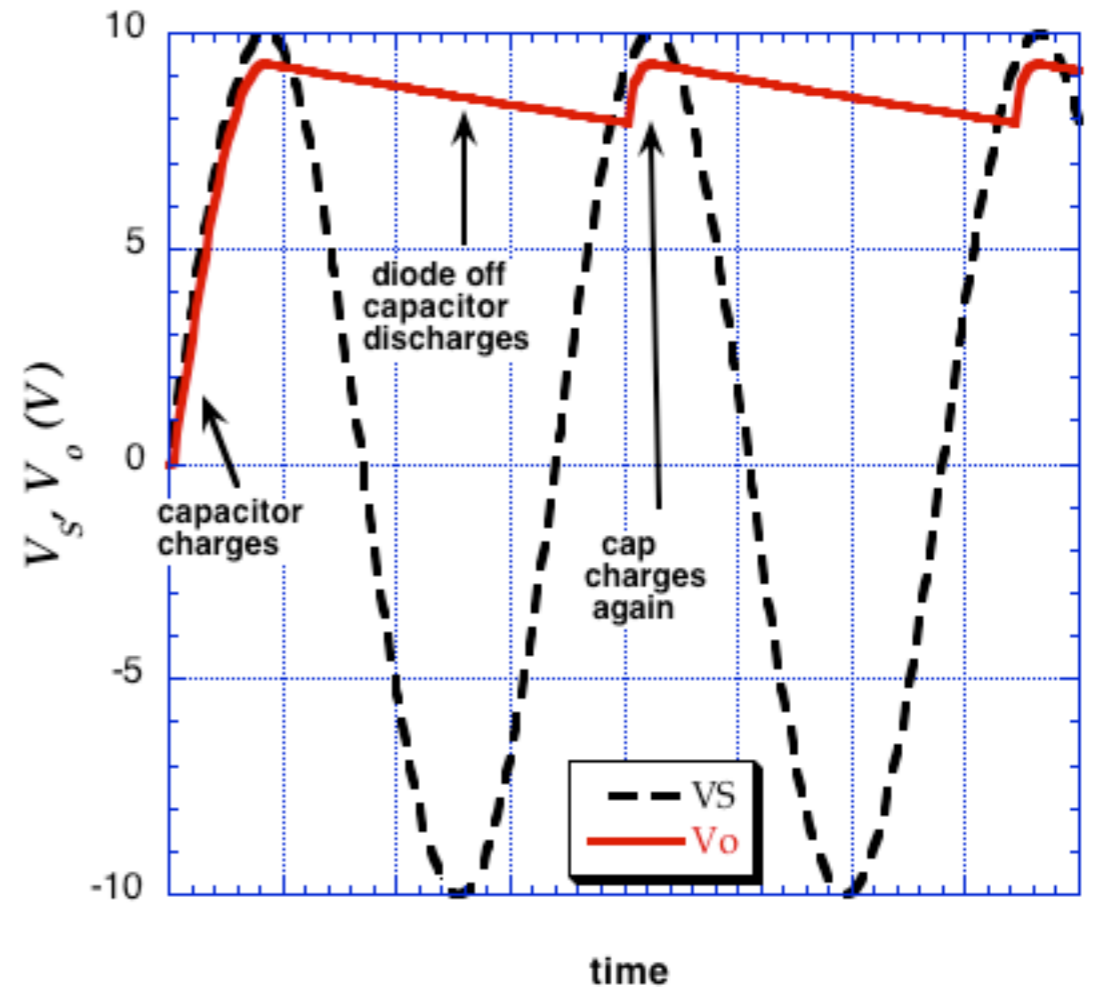
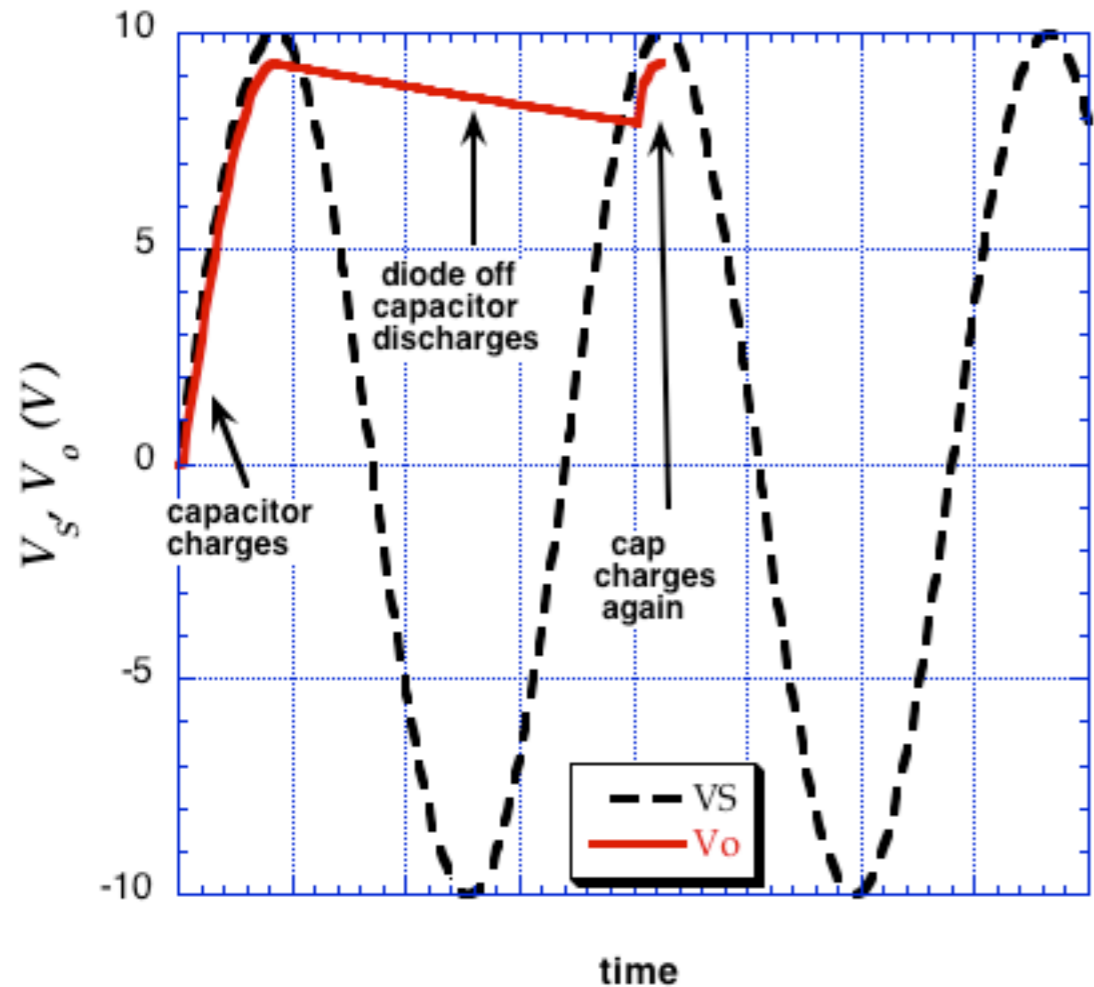
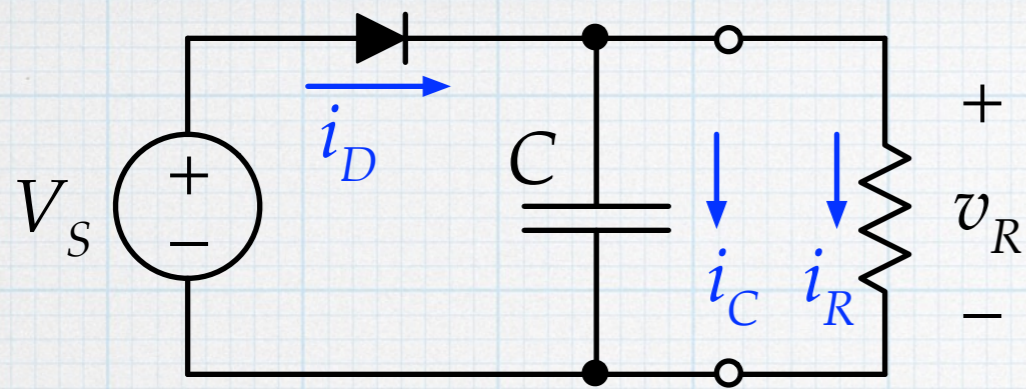
Peak rectifier

Add a largish capacitor after the diode, in parallel with the load.



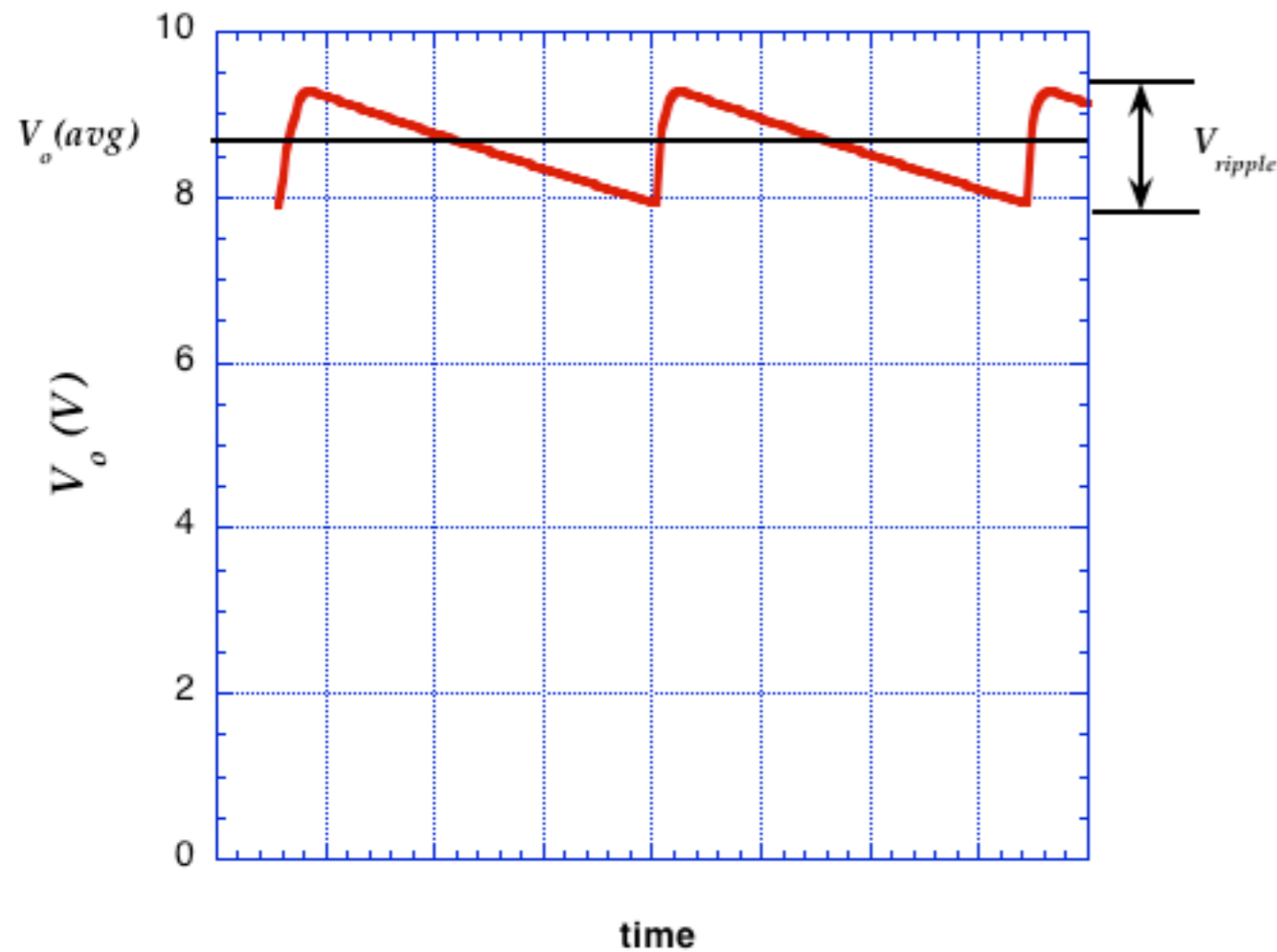
Initially, diode is on & cap charges to $V_P - 0.7$ V.

While $V_S < v_C$, diode is off!
Cap discharges through load.



Diode stay off until V_S comes back around and becomes bigger than v_C . Then diode comes on again and re-charges the capacitor.

When V_S falls to less than v_C , the diode turn off again, and the cycle continues.



Not a perfect DC voltage at output. There is some variation (ripple) around an average value.

$$V_o(\max) = V_P - 0.7V$$

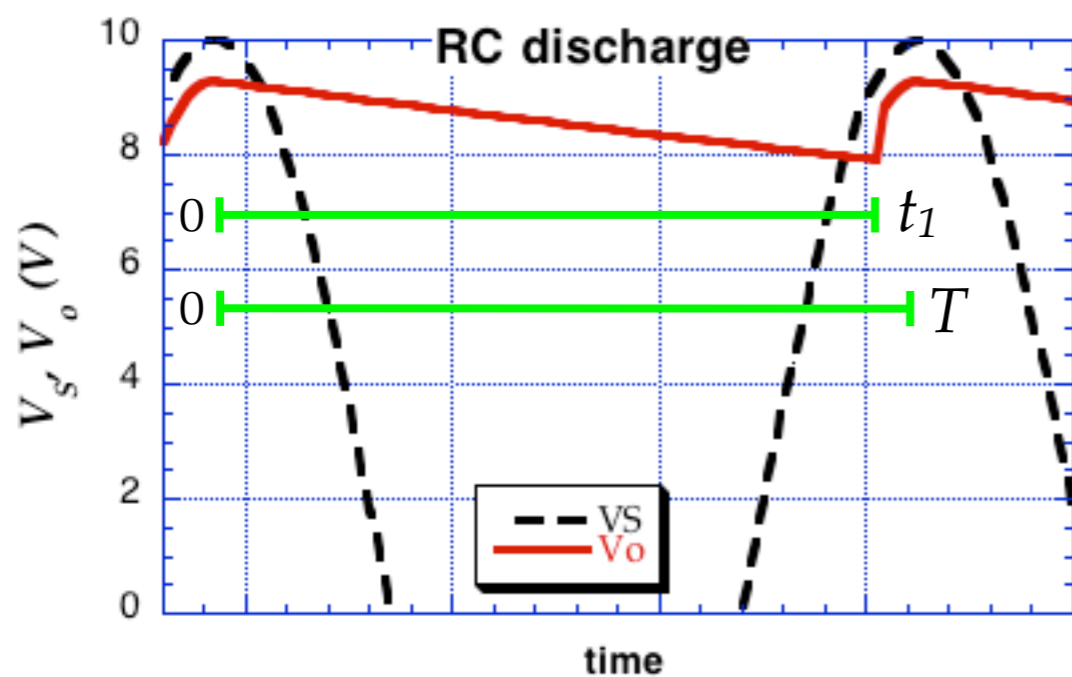
$$V_o(\min) = [V_P - 0.7V] \exp\left(-\frac{t_1}{RC}\right)$$

$$\approx [V_P - 0.7V] \exp\left(-\frac{T}{RC}\right)$$

$$V_{ripple} = V_o(\max) - V_o(\min)$$

$$= [V_P - 0.7V] \left[1 - \exp\left(-\frac{T}{RC}\right)\right]$$

$$V_o(\text{avg}) \approx V_o(\max) - \frac{V_{ripple}}{2}$$



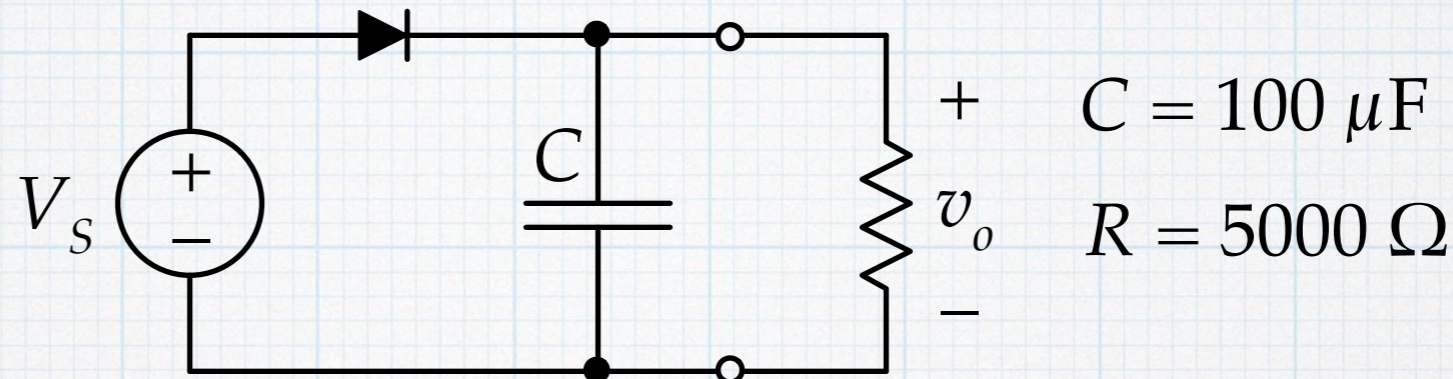
t_1 = time when diode conducts again.

$$t_1 \approx T$$

Example 1

$$V_S = (15\text{V}) \sin\left(\frac{2\pi}{T}t\right)$$

$$T = 16.67 \text{ ms}$$



Find the average value of v_o and the ripple voltage. Repeat for $R = 1000 \Omega$ and 200Ω .

$$\begin{aligned} V_{ripple} &= [V_P - 0.7\text{V}] \left[1 - \exp\left(-\frac{T}{RC}\right) \right] \\ &= [15\text{V} - 0.7\text{V}] \left[1 - \exp\left(-\frac{16.67\text{ms}}{(5000\Omega)(100\mu\text{F})}\right) \right] \\ &= 0.47 \text{ V} \end{aligned}$$

$$V_o(\text{avg}) = V_o(\text{max}) - \frac{V_{ripple}}{2} = 14.3\text{V} - \frac{0.47\text{V}}{2} = 14.1\text{V}$$

$$R = 1 \text{ k}\Omega$$

$$V_{ripple} = 2.19 \text{ V}$$

$$V_o(\text{avg}) = 13.2 \text{ V}$$

$$R = 200 \Omega$$

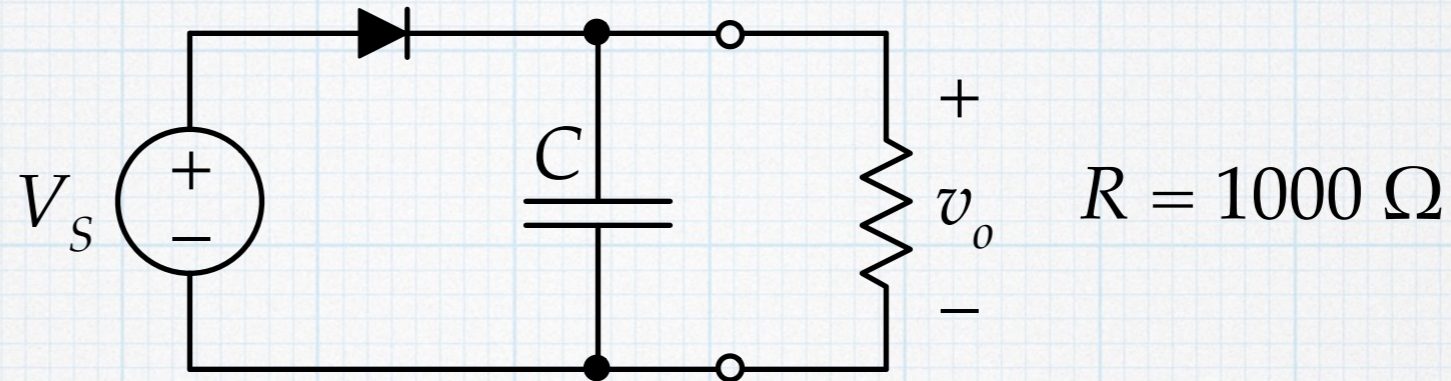
$$V_{ripple} = 8.09 \text{ V}$$

$$V_o(\text{avg}) = 10.2 \text{ V}$$

Drawing more current causes the ripple to increase and V_{DC} to droop. Can fight this with more capacitance.

Example 2

$$V_S = (25\text{V}) \sin\left(\frac{2\pi}{T}t\right)$$



$$T = 16.67\ \text{ms}$$

Find the capacitance so that the ripple will be no bigger than 1 V.

What is the DC voltage?

$$V_{\text{ripple}} = [V_P - 0.7\text{V}] \left[1 - \exp\left(-\frac{T}{RC}\right) \right]$$

$$C = -\frac{T}{R} \left[\ln\left(1 - \frac{V_{\text{ripple}}}{V_P - 0.7\text{V}}\right) \right]^{-1} = -\frac{16.67\text{ms}}{1000\Omega} \left[\ln\left(1 - \frac{1\text{V}}{24.3\text{V}}\right) \right]^{-1} = 397\ \mu\text{F}$$

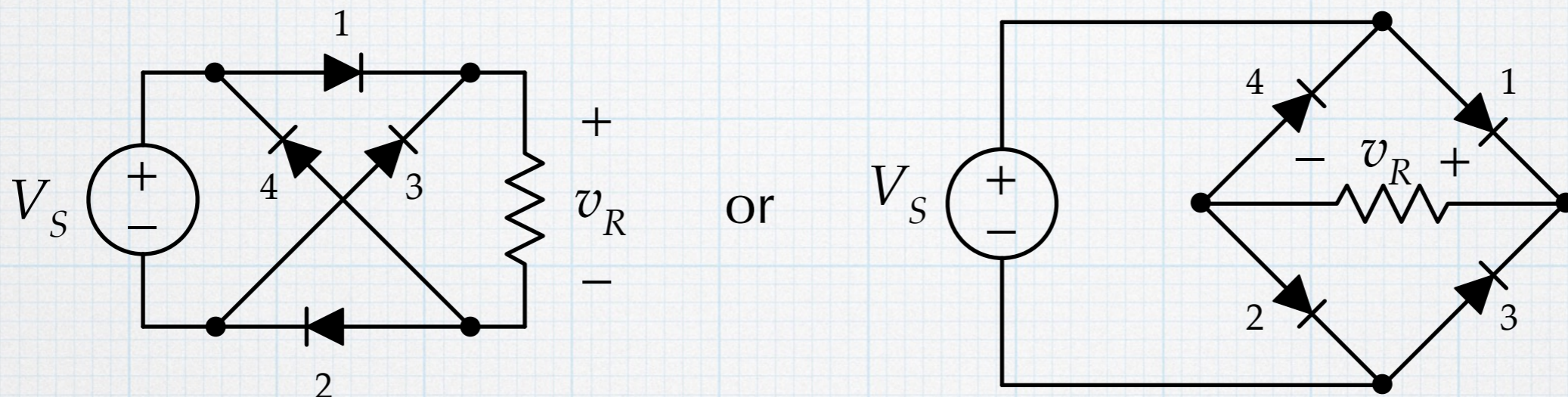
$$V_o(\text{avg}) = V_o(\text{max}) - \frac{V_{\text{ripple}}}{2} = 24.3\text{V} - \frac{1\text{V}}{2} = 23.8\text{V}$$

What capacitance is needed to limit the ripple to 0.1 V?

$$C = 4000\ \mu\text{F} \quad !!!$$

Full-wave rectifier

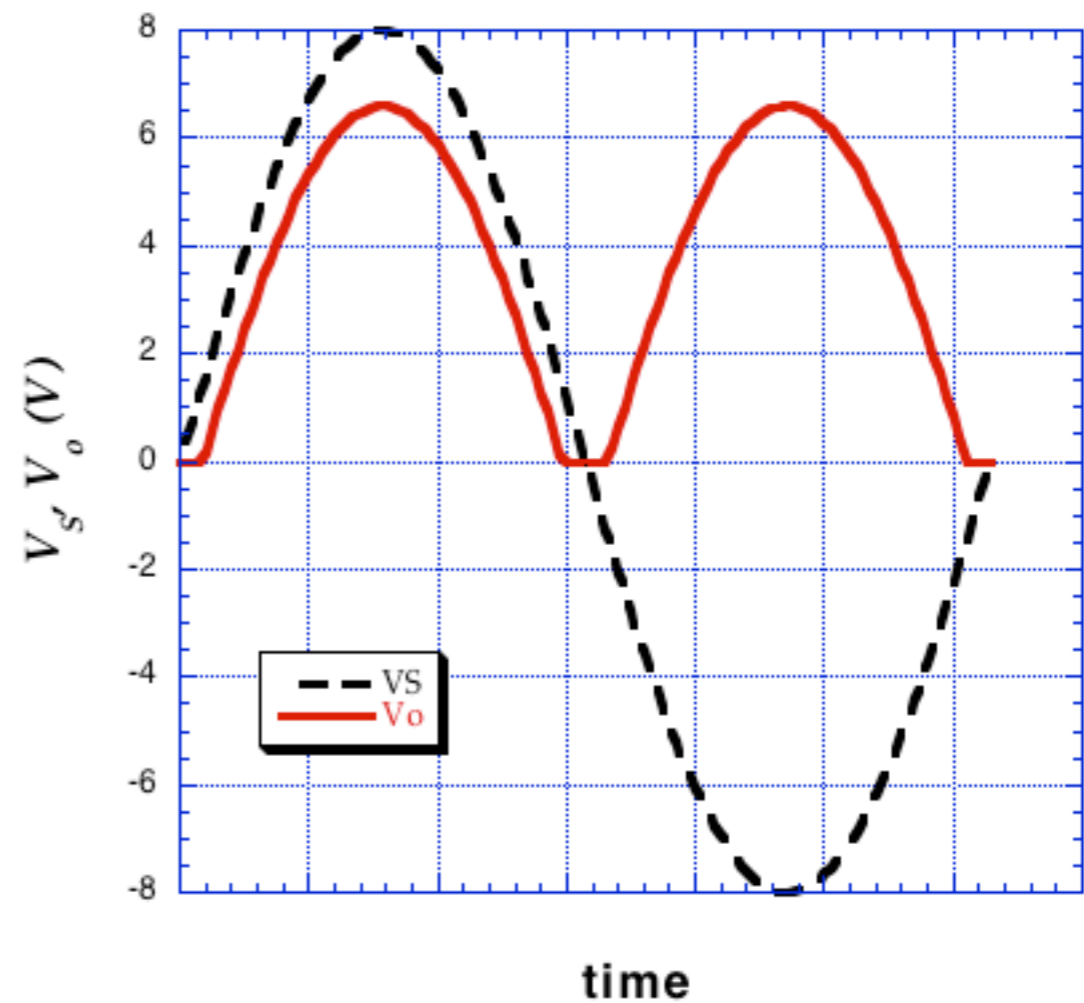
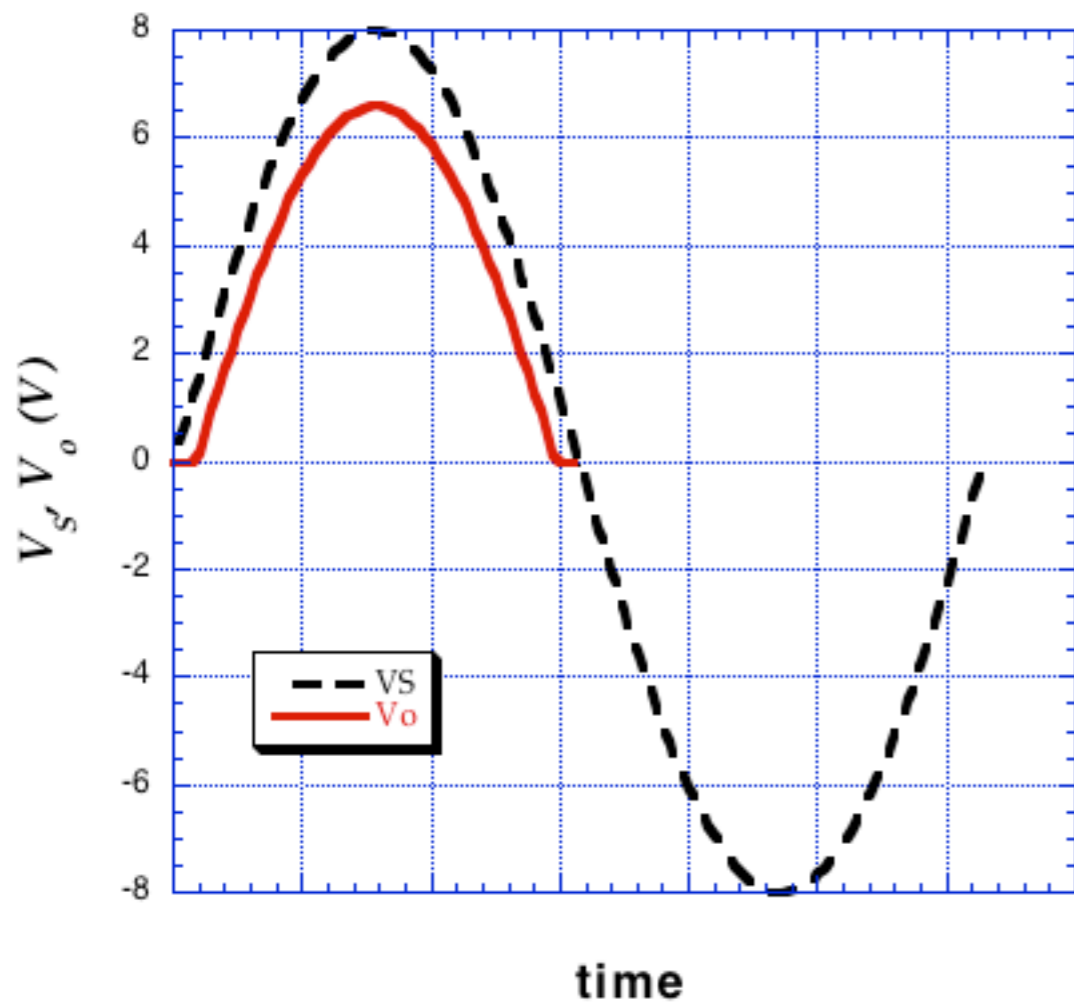
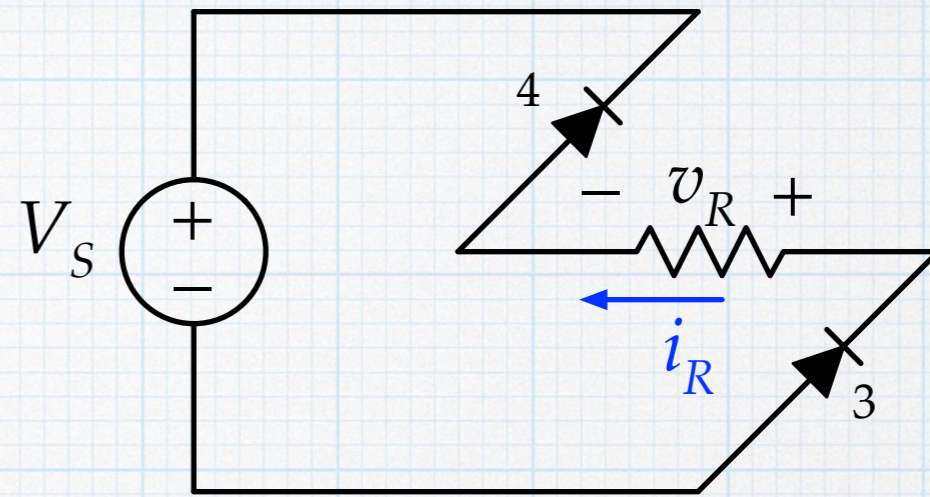
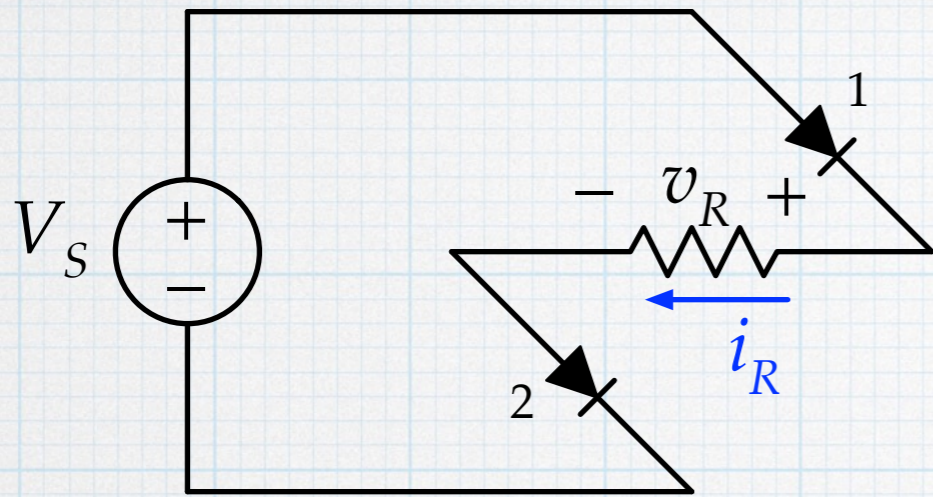
With a few more diodes, we can rectify the entire sinusoidal input.



The diodes are in a bridge configuration.

During the positive half cycle of the input, diodes 1 and 2 will be forward biased. Current will flow from the positive source through those diodes and the resistor to generate a positive voltage across the resistor.

During the negative half cycle of the input, diodes 3 and 4 will be forward biased. Current will flow from the negative source through those diodes and the resistor to generate a positive voltage across the resistor, again.



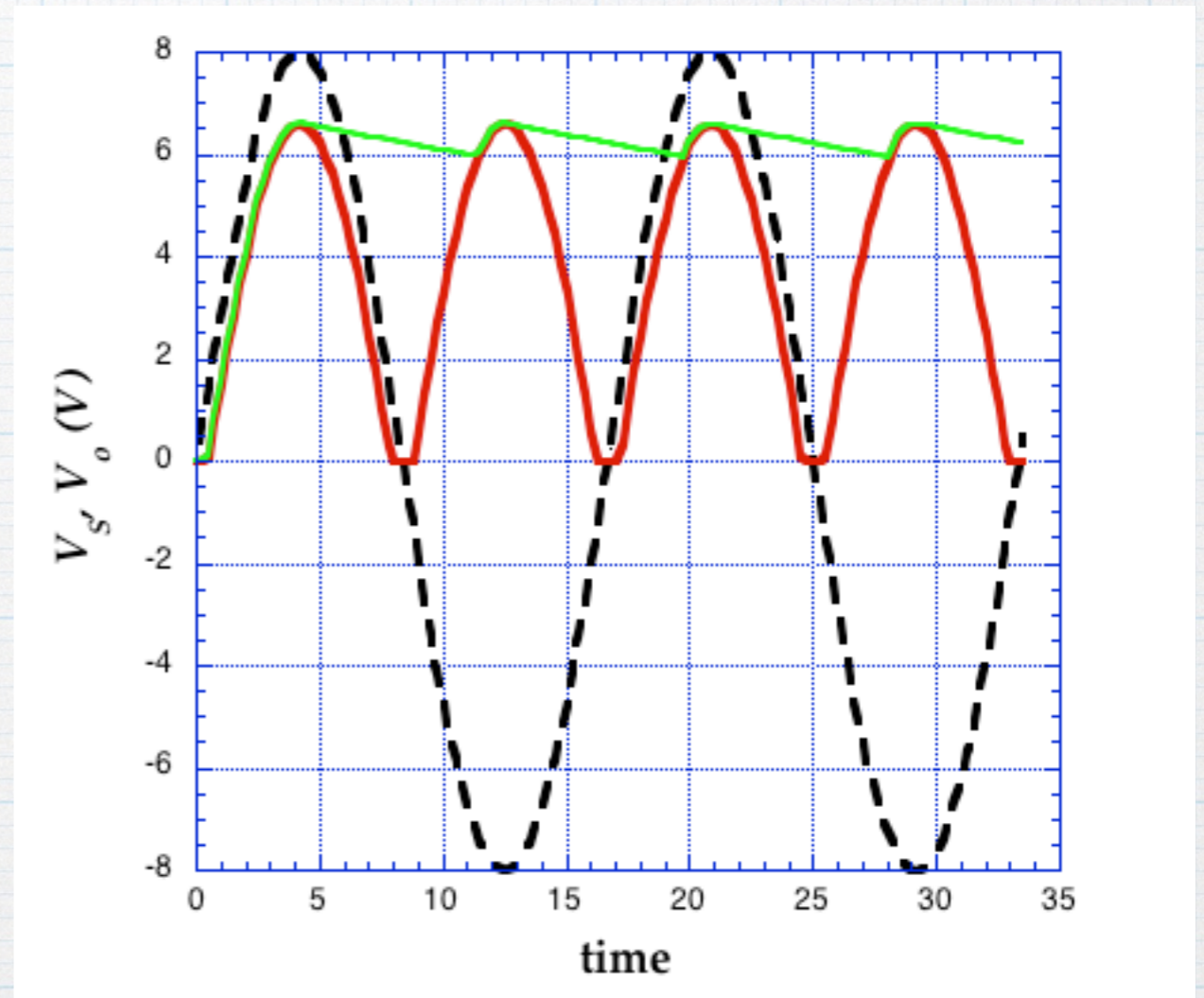
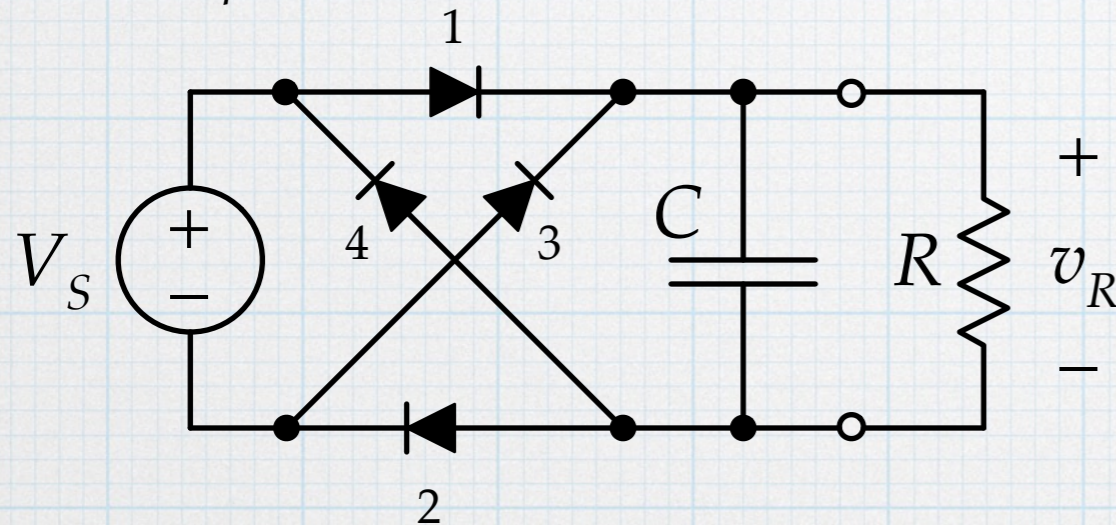
Note that there are no two diode drops in the conduction path(s).
Also, the frequency is effectively doubled.

Full-wave peak rectifier

Placing a capacitor in parallel with the load, turns the circuit into a full-wave peak rectifier. It behaves essentially the same as the half-wave peak rectifier except with twice the frequency (half the period).

$$V_S(t) = V_p \sin\left(\frac{2\pi}{T}t\right)$$

$$V_p = 8 \text{ V.}$$



The ripple voltage is calculated in exactly the same way, except that the period is cut in half (frequency doubled).

$$V_{ripple} = [V_P - 1.4\text{V}] \left[1 - \exp\left(-\frac{T}{2RC}\right) \right]$$

Same as doubling capacitance!

Example 3

You want to use a wall transformer that produces $10\text{-}V_{\text{RMS}}$ at the secondary to generate a DC voltage. The desired voltage DC should be greater than 12 V and it should be able to supply at least 50 mA while keeping the voltage ripple to less than 5% . Design the rectifier to meet these goals. (Note: $f = 60\text{ Hz}$.)

$10\text{ }V_{\text{RMS}} \rightarrow 14.1\text{ V}$ amplitude

effective $R_L \approx V_o / I_o = 12.0\text{ V} / (50\text{ mA}) = 240\ \Omega$

Note: This would be the minimum value of effective resistance. If we choose C to meet the ripple requirement, then we will still be safe if we use a slightly higher V_o .

Two options: half-wave or full-wave rectifier. Try both.

Half-wave:

$$V_o(\text{max}) = V_p - 0.7\text{ V} = 13.4\text{ V} \rightarrow V_{\text{ripple}} \leq 0.67\text{ V}.$$

$$C = -\frac{T}{R} \left[\ln \left(1 - \frac{V_{\text{ripple}}}{V_p - 0.7\text{V}} \right) \right]^{-1} = 1350\ \mu\text{F}$$

$$V_o(\text{avg}) = V_o(\text{max}) - V_{\text{ripple}} / 2 = 13.06\text{ V}.$$

Full-wave:

$$V_o(\text{max}) = V_p - 2(0.7 \text{ V}) = 12.74 \text{ V} \rightarrow V_{\text{ripple}} \leq 0.64 \text{ V.}$$

$$C = -\frac{T}{2R} \left[\ln \left(1 - \frac{V_{\text{ripple}}}{V_o(\text{max})} \right) \right]^{-1} = 673 \mu\text{F}$$

$$V_o(\text{avg}) = V_o(\text{max}) - V_{\text{ripple}} / 2 = 12.42 \text{ V.}$$

Either approach will work and meet the requirements. The full-wave version uses extra diodes, but only half the capacitance. Since diodes are nearly free (pennies per piece), but big capacitors are relatively expensive, the full-wave circuit will actually cost less than the half-wave.

This is why full-wave rectifiers are used more commonly than half-wave rectifiers.

Component manufactures supply full-wave bridge rectifiers packaged as single unit with the transformer sinusoid as input the rectified waveform as the output.